Problem 39

Tectonic plates are large segments of Earth's crust that move slowly. Suppose one such plate has an average speed of 4.0 cm/yr. (a) What distance does it move in 1.0 s at this speed? (b) What is its speed in kilometers per million years?

Solution

Part (a)

Multiply the given speed by the appropriate conversion factors to get the desired units.

$$4.0 \frac{\mathrm{cm}}{\mathrm{yr}} = 4.0 \frac{\mathrm{cm}}{\mathrm{yr}} \times \frac{1}{365} \frac{\mathrm{yr}}{\mathrm{days}} \times \frac{1}{24} \frac{\mathrm{day}}{\mathrm{k}} \times \frac{1}{60} \frac{\mathrm{km}}{\mathrm{min}} \times \frac{1}{60} \frac{\mathrm{min}}{\mathrm{s}} \approx 1.3 \times 10^{-7} \frac{\mathrm{cm}}{\mathrm{s}}$$

In 1.0 s the distance the plate moves is roughly

$$1.3 \times 10^{-7} \text{ cm} = 1.3 \times 10^{-7} \text{ cm} \times \frac{1 \text{ lm}}{100 \text{ cm}} \times \frac{10^9 \text{ nm}}{1 \text{ lm}} = 1.3 \text{ nm}.$$

Part (b)

Multiply the given speed by the appropriate conversion factors to get the desired units.

$$4.0 \; \frac{\rm cm}{\rm yr} = 4.0 \; \frac{\rm cm}{\rm yr} \times \frac{1 \; \rm km}{100 \; \rm cm} \times \frac{1 \; \rm km}{1000 \; \rm kg} = 4.0 \times 10^{-5} \; \frac{\rm km}{\rm yr}$$

The speed in kilometers per million years is then

$$4.0 \times 10^{-5} \frac{\text{km}}{\text{vr}} \times \frac{10^6}{10^6} = 4.0 \times 10^1 \frac{\text{km}}{10^6 \text{ vrs}} = 40 \frac{\text{km}}{10^6 \text{ vrs}}.$$